

BER of a multiple antenna
wireless system with L
antennas,

$$\text{BER} = \left(\frac{1-\lambda}{2} \right)^L \sum_{l=0}^{L-1} \frac{L-l-1}{L+l-1} C_l \left(\frac{1+\lambda}{2} \right)^l$$

$$\lambda = \sqrt{\frac{\text{SNR}}{2+\text{SNR}}}$$

Develop an approximation
for BER in a multiple
antenna wireless system

$$\frac{1-\lambda}{2} = \frac{1}{2} (1-\lambda)$$
$$= \frac{1}{2} \left(1 - \sqrt{\frac{\text{SNR}}{2+\text{SNR}}} \right)$$

$$= \frac{1}{2} \left(1 - \sqrt{\frac{1}{1 + \frac{2}{\text{SNR}}}} \right)$$

$$= \frac{1}{2} \left(1 - \left(1 + \frac{2}{\text{SNR}} \right)^{-\frac{1}{2}} \right)$$

if $x \approx 0$

$$(1+x)^{-\frac{1}{2}} \approx 1 - \frac{1}{2}x$$

$$\approx \frac{1}{2} \left(1 - \left(1 - \frac{1}{2} \cdot \frac{2}{\text{SNR}} \right) \right)$$

$$= \frac{1}{2} \cdot \frac{1}{\text{SNR}} = \frac{1}{2 \cdot \text{SNR}}$$

$$\frac{1+\lambda}{2} = \frac{1}{2} \left(1 + \sqrt{\frac{\text{SNR}}{2+\text{SNR}}} \right)$$

$$= \frac{1}{2} \left(1 + \sqrt{\frac{1}{1 + \frac{2}{\text{SNR}}}} \right)$$

$$= \frac{1}{2} \left(1 + \left(1 + \frac{2}{\text{SNR}} \right)^{-1/2} \right)$$

$$\approx \frac{1}{2} \left(1 + \left(1 - \frac{1}{2} \cdot \frac{2}{\text{SNR}} \right) \right)$$

$$= \frac{1}{2} \left(2 - \frac{1}{\text{SNR}} \right)$$



$\frac{1}{\text{SNR}} \approx 0$ at high SNR

$$\approx \frac{1}{2} \times 2 = 1$$

Therefore, at high SNR

$$\frac{1-\lambda}{2} \approx \frac{1}{2 \cdot \text{SNR}}$$

$$\frac{1+\lambda}{2} \approx 1$$

$$BER = \left(\frac{1-\lambda}{2} \right)^L \sum_{l=0}^{L-1} \binom{L+l-1}{l} \left(\frac{1+\lambda}{2} \right)^l$$

at high
SNR
 $\lambda \approx$

$$\left(\frac{1}{2 \cdot SNR} \right)^L \sum_{l=0}^{L-1} \binom{L+l-1}{l} \cdot 1$$

$$\approx \left(\frac{1}{2 \cdot SNR} \right)^L \sum_{l=0}^{L-1} \binom{L+l-1}{l}$$

$$= 2^{L-1} \binom{2L-1}{L} \left(\frac{1}{2 \cdot SNR} \right)^L$$

At high SNR, BER of
wireless communication
system with L antennas,

$$\text{Approx BER} = 2^{L-1} C_L \left(\frac{1}{2 \text{SNR}} \right)^L$$

For $L = 2$

Approx BER

$$= 2^{L-1} C_L \cdot \left(\frac{1}{2 \text{SNR}} \right)^L$$

$$= 3 C_2 \cdot \left(\frac{1}{2 \text{SNR}} \right)^2$$

$$= 3 \cdot \frac{1}{4} \cdot \frac{1}{\text{SNR}^2} = \frac{3}{4} \cdot \frac{1}{\text{SNR}^2}$$

↑
Approx BER
for $L = 2$